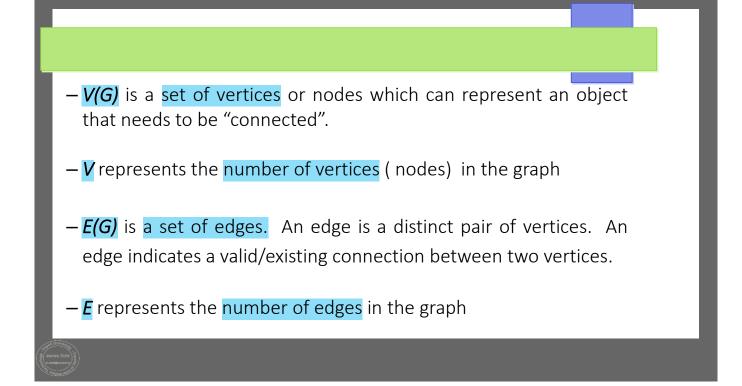


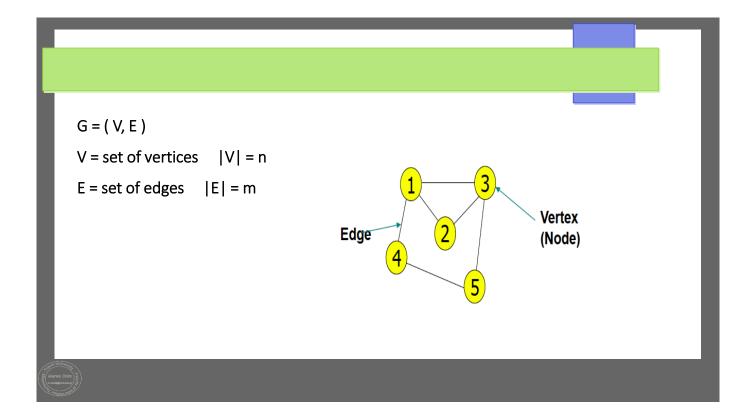
## **Graph Algorithms**

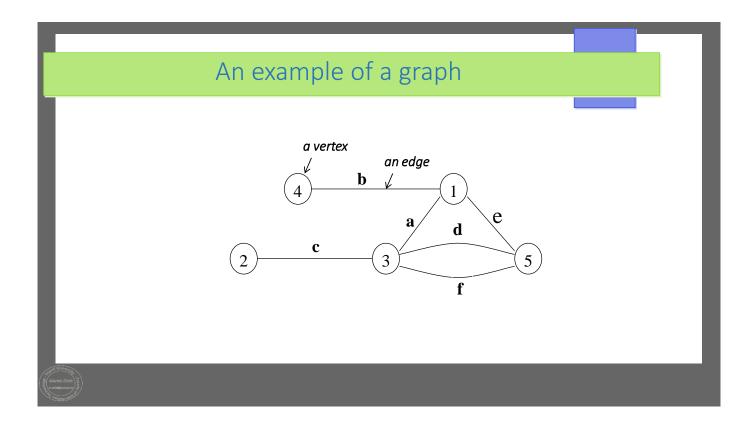
## What is a Graph?

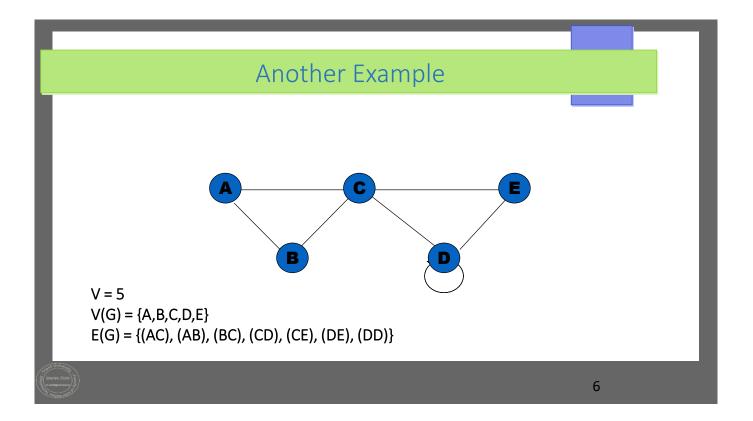
A Graph is a abstract data structure represents a collection of items with pairwise relationship between these items.

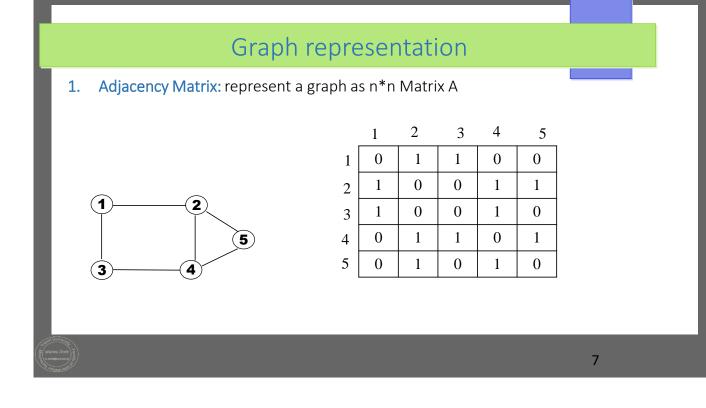
It consists of a set of vertices (nodes) connected by a set of edges (links), and is denoted by G = (V, E), where V is set of vertices and E is set of edges.

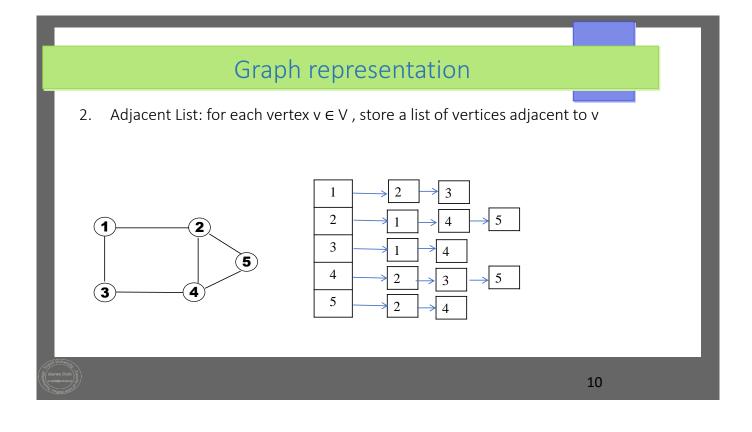


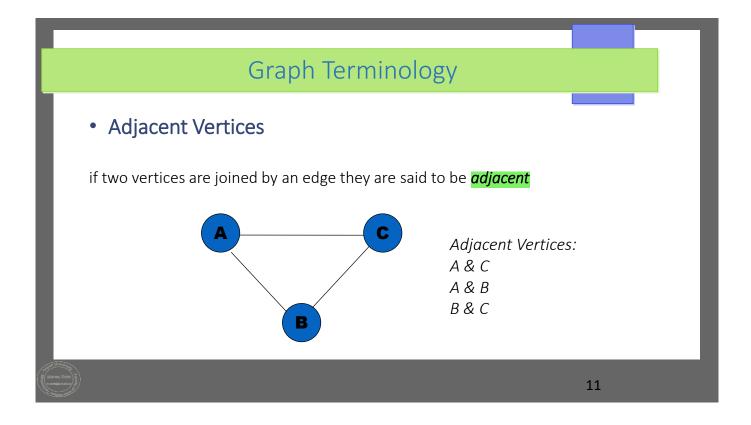


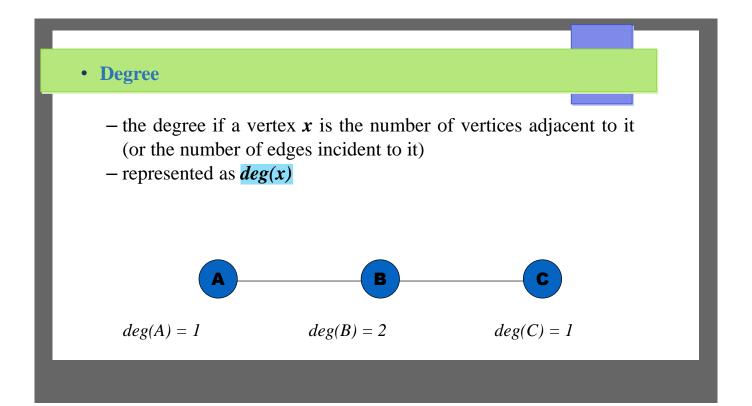


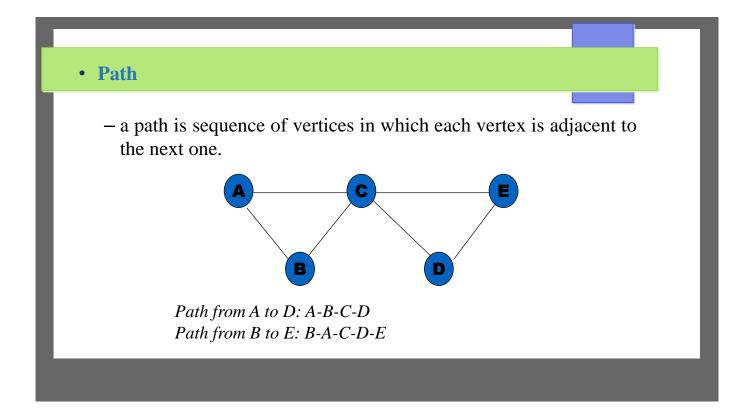


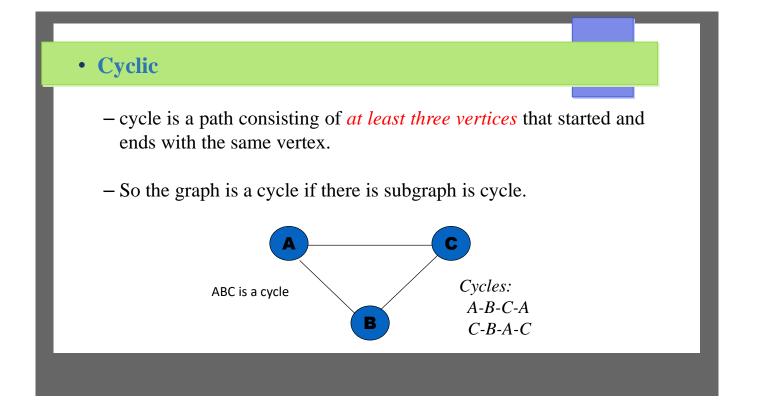


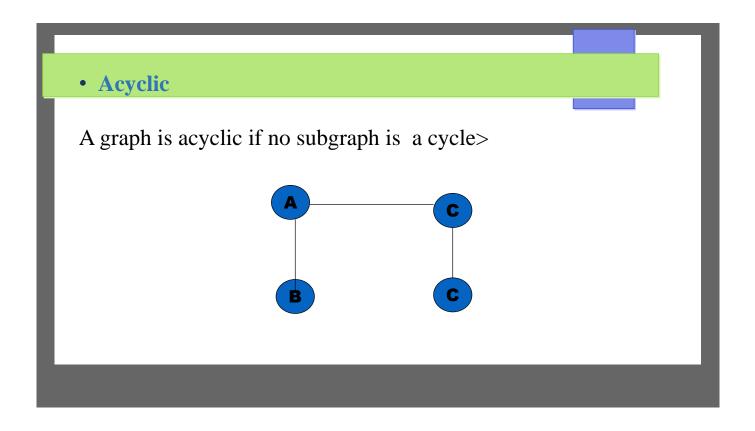


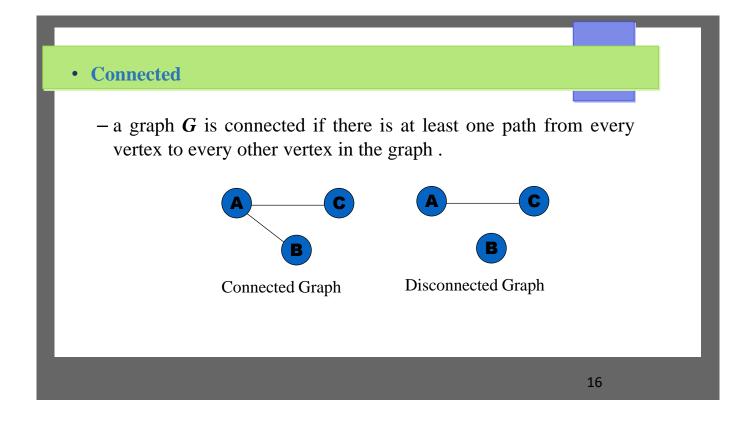


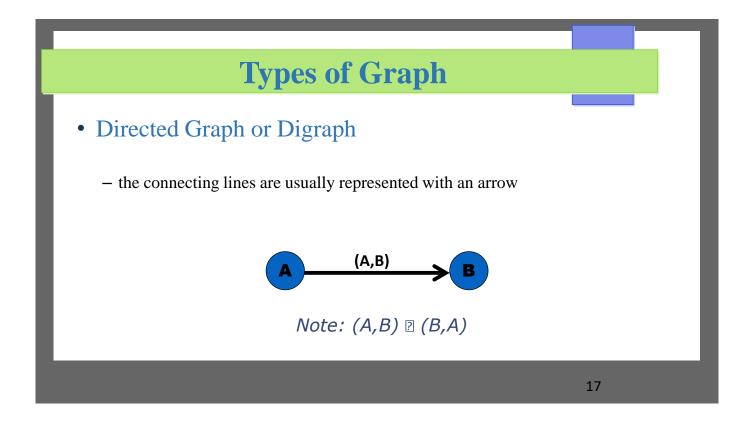


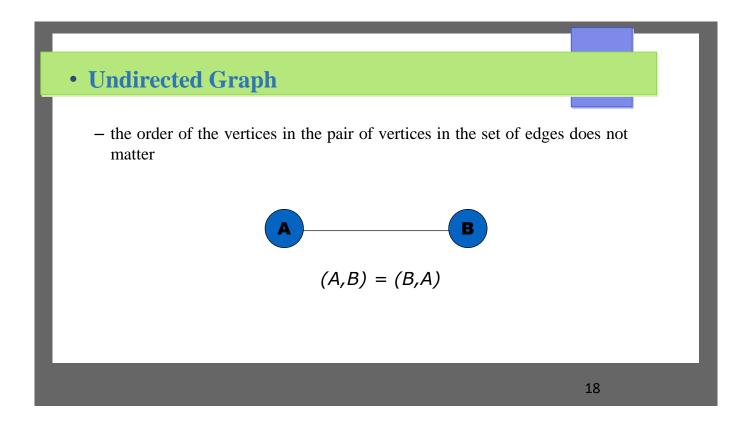


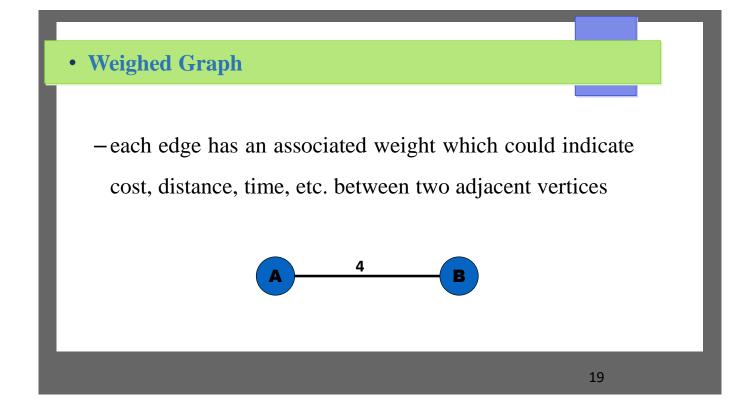


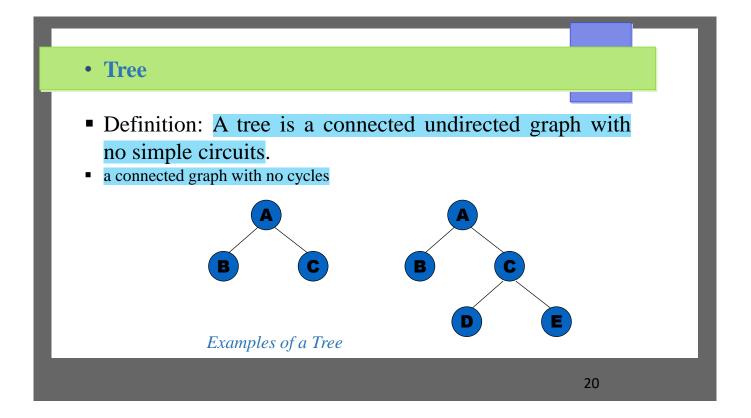


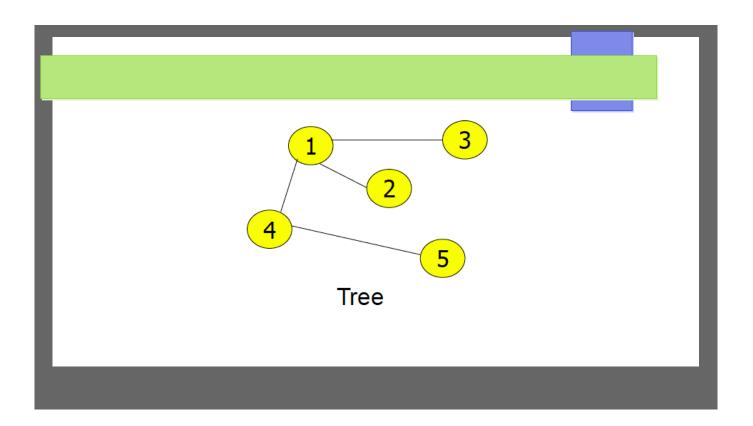


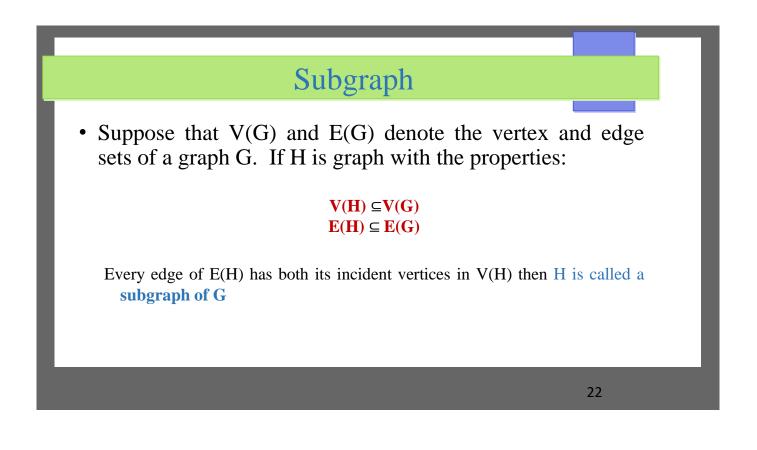


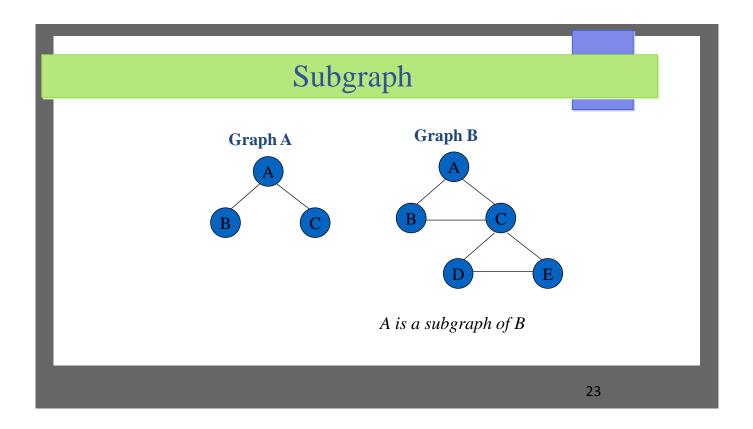


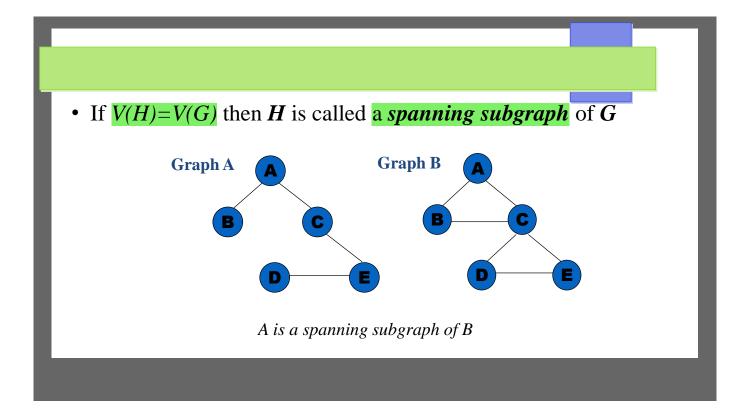


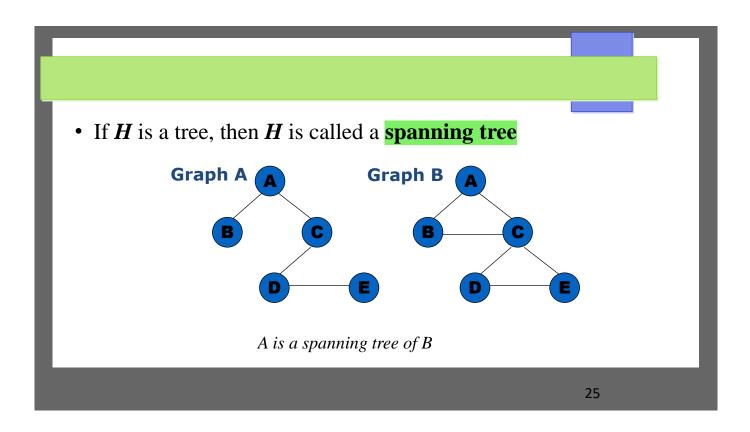


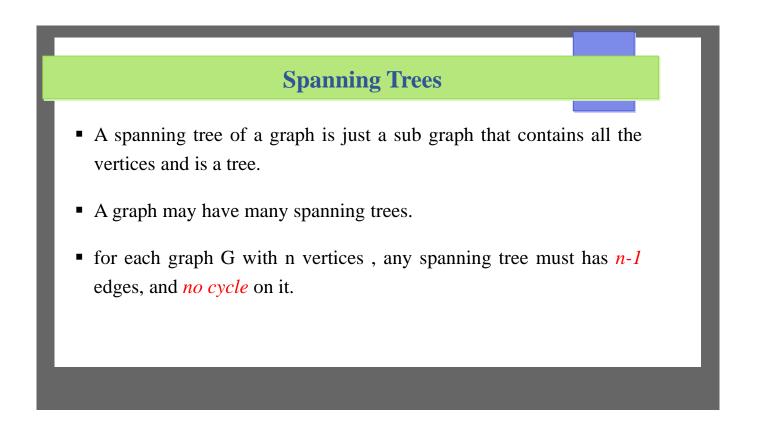








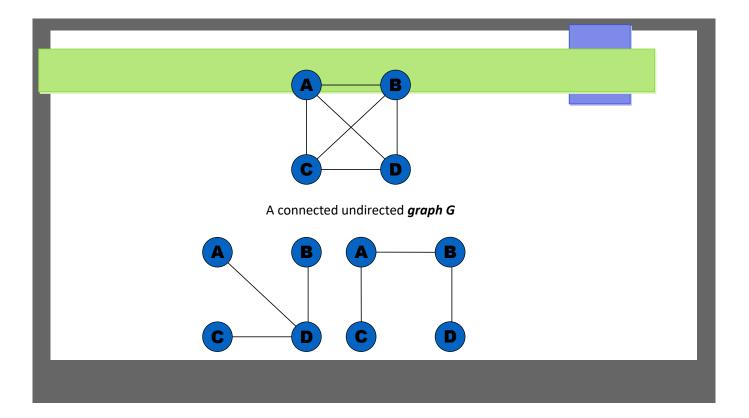


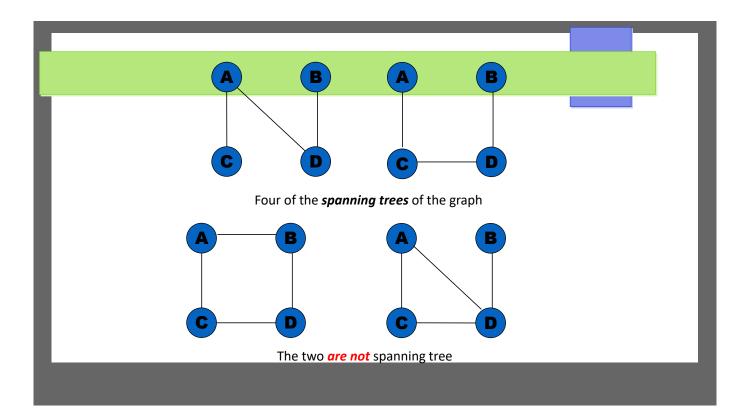


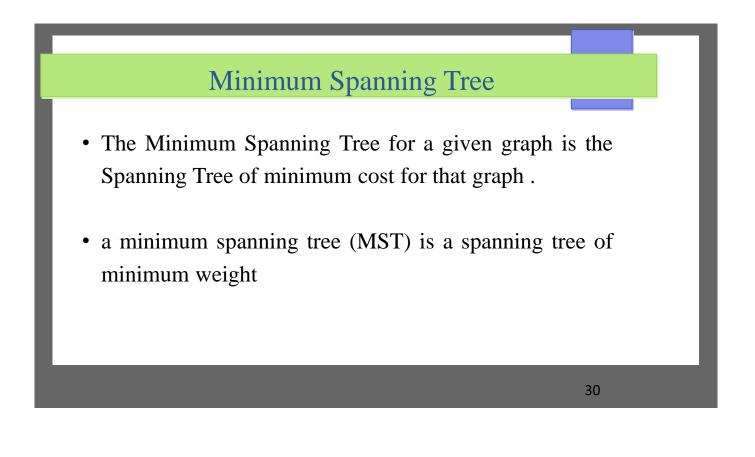
## **Spanning Tree properties:**

On a connected graph G=(V, E), a spanning tree *must be*:

- a connected subgraph (contains all vertices of G)
- no cycle.
- is a tree (|E| = |V| 1)

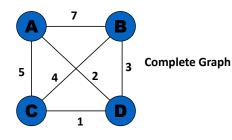






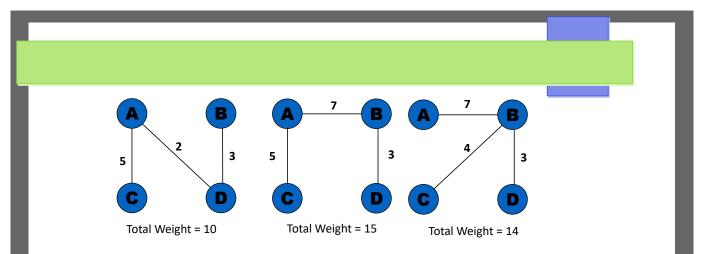
Note : we need to have spanning tree that connected to all its vertices but has less weights.

Example:



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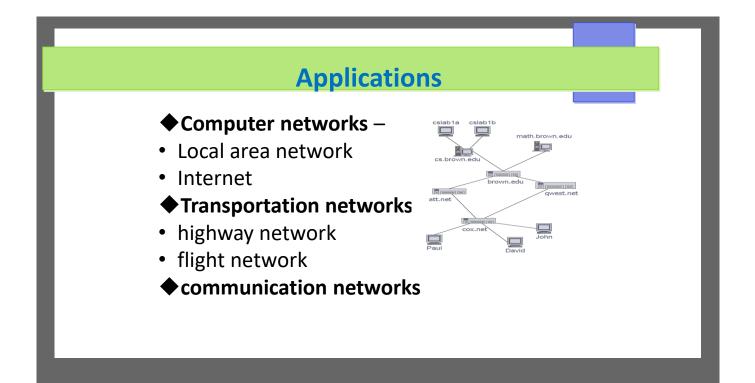
Note: Number of spanning tree of complete graph =  $n^{n-2}$ 



All These subgraphs are spanning tree, all its vertices are connected and there is no cycle. But, they are not minimum spanning tree because the total weights are not the least total weight.

## **MST** Algorithms

 Minimum Spanning Tree –Kruskal's Algorithm –Primm's Algorithm



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